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In[2]:= << C:\drorbn\AcademicPensieve\Projects\Mathematica\LinAlg.m

In[3]:= rrt1 = Total[(Signature[#] * (P1@#)) & /@ Permutations[{1, 2, 3}]];
rrt = Expand[rrt1 * (rrt1 /. P1 -> P2)] /. P1[p1_] P2[p2_] -> (
  P@@(p1~Join~(p2+3)) - P@@((p1+3)~Join~p2)
)

Out[4]= P[1, 2, 3, 4, 5, 6] - P[1, 2, 3, 4, 6, 5] - P[1, 2, 3, 5, 4, 6] + P[1, 2, 3, 5, 6, 4] +
  P[1, 2, 3, 6, 4, 5] - P[1, 2, 3, 6, 5, 4] - P[1, 3, 2, 4, 5, 6] + P[1, 3, 2, 4, 6, 5] +
  P[1, 3, 2, 5, 4, 6] - P[1, 3, 2, 5, 6, 4] - P[1, 3, 2, 6, 4, 5] + P[1, 3, 2, 6, 5, 4] -
  P[2, 1, 3, 4, 5, 6] + P[2, 1, 3, 4, 6, 5] + P[2, 1, 3, 5, 4, 6] - P[2, 1, 3, 5, 6, 4] -
  P[2, 1, 3, 6, 4, 5] + P[2, 1, 3, 6, 5, 4] + P[2, 3, 1, 4, 5, 6] - P[2, 3, 1, 4, 6, 5] -
  P[2, 3, 1, 5, 4, 6] + P[2, 3, 1, 5, 6, 4] + P[2, 3, 1, 6, 4, 5] - P[2, 3, 1, 6, 5, 4] +
  P[3, 1, 2, 4, 5, 6] - P[3, 1, 2, 4, 6, 5] - P[3, 1, 2, 5, 4, 6] + P[3, 1, 2, 5, 6, 4] +
  P[3, 1, 2, 6, 4, 5] - P[3, 1, 2, 6, 5, 4] - P[3, 2, 1, 4, 5, 6] + P[3, 2, 1, 4, 6, 5] +
  P[3, 2, 1, 5, 4, 6] - P[3, 2, 1, 5, 6, 4] - P[3, 2, 1, 6, 4, 5] + P[3, 2, 1, 6, 5, 4] -
  P[4, 5, 6, 1, 2, 3] + P[4, 5, 6, 1, 3, 2] + P[4, 5, 6, 2, 1, 3] - P[4, 5, 6, 2, 3, 1] -
  P[4, 5, 6, 3, 1, 2] + P[4, 5, 6, 3, 2, 1] + P[4, 6, 5, 1, 2, 3] - P[4, 6, 5, 1, 3, 2] -
  P[4, 6, 5, 2, 1, 3] + P[4, 6, 5, 2, 3, 1] + P[4, 6, 5, 3, 1, 2] - P[4, 6, 5, 3, 2, 1] +
  P[5, 4, 6, 1, 2, 3] - P[5, 4, 6, 1, 3, 2] - P[5, 4, 6, 2, 1, 3] + P[5, 4, 6, 2, 3, 1] +
  P[5, 4, 6, 3, 1, 2] - P[5, 4, 6, 3, 2, 1] - P[5, 6, 4, 1, 2, 3] + P[5, 6, 4, 1, 3, 2] +
  P[5, 6, 4, 2, 1, 3] - P[5, 6, 4, 2, 3, 1] - P[5, 6, 4, 3, 1, 2] + P[5, 6, 4, 3, 2, 1] -
  P[6, 4, 5, 1, 2, 3] + P[6, 4, 5, 1, 3, 2] + P[6, 4, 5, 2, 1, 3] - P[6, 4, 5, 2, 3, 1] -
  P[6, 4, 5, 3, 1, 2] + P[6, 4, 5, 3, 2, 1] + P[6, 5, 4, 1, 2, 3] - P[6, 5, 4, 1, 3, 2] -
  P[6, 5, 4, 2, 1, 3] + P[6, 5, 4, 2, 3, 1] + P[6, 5, 4, 3, 1, 2] - P[6, 5, 4, 3, 2, 1]

In[5]:= lam4[l_List] := Total[
  (P[1, 2, 3, 4, 5, 6] /. Thread[l -> #]) & /@ Permutations[l]) /.
  p_P -> Signature[p] * p
];
lam4[i_, j_] := lam4[Complement[Range[6], {i, j}]];

In[7]:= lam4[3, 5]

Out[7]= P[1, 2, 3, 4, 5, 6] - P[1, 2, 3, 6, 5, 4] - P[1, 4, 3, 2, 5, 6] + P[1, 4, 3, 6, 5, 2] +
  P[1, 6, 3, 2, 5, 4] - P[1, 6, 3, 4, 5, 2] - P[2, 1, 3, 4, 5, 6] + P[2, 1, 3, 6, 5, 4] +
  P[2, 4, 3, 1, 5, 6] - P[2, 4, 3, 6, 5, 1] - P[2, 6, 3, 1, 5, 4] + P[2, 6, 3, 4, 5, 1] +
  P[4, 1, 3, 2, 5, 6] - P[4, 1, 3, 6, 5, 2] - P[4, 2, 3, 1, 5, 6] + P[4, 2, 3, 6, 5, 1] +
  P[4, 6, 3, 1, 5, 2] - P[4, 6, 3, 2, 5, 1] - P[6, 1, 3, 2, 5, 4] + P[6, 1, 3, 4, 5, 2] +
  P[6, 2, 3, 1, 5, 4] - P[6, 2, 3, 4, 5, 1] - P[6, 4, 3, 1, 5, 2] + P[6, 4, 3, 2, 5, 1]

In[8]:= AllPs = (P@@#) & /@ Permutations[{1, 2, 3, 4, 5, 6}];

In[9]:= LC2SA[AllPs, {lam4[3, 5]}]

Out[9]= SparseArray[<24>, {1, 720}]

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